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# ABCluster Manual

Version 1.3

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[http://www.uni-koeln.de/math-nat-fak/tcchem/mitarbeiter/  
zhang/zhang/software-abcluster-introduction.html](http://www.uni-koeln.de/math-nat-fak/tcchem/mitarbeiter/zhang/zhang/software-abcluster-introduction.html)

ABCluster: A software for the global optimization of atomic and  
molecular clusters by the artificial bee colony algorithm



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# Chapter 1

## Introduction to ABCluster

### 1.1 What is ABCluster?

Briefly, ABCluster searches the **global** as well as the **local** minima of atomic and molecular clusters.

ABCluster is a software developed by Dr. Jun Zhang to perform the global optimization of atomic and molecular clusters. It is an efficient and user-friendly program. It is designed in a way that non-experts as well as experts can perform a global optimization readily without knowing too much about the internal algorithm (being a black-box).

The latest version of ABCluster, and a lot of resources can be obtained from the web page:

<http://www.uni-koeln.de/math-nat-fak/tcchem/mitarbeiter/zhang/zhang/software-abcluster-introduction.html>

ABCluster is written in standard C++ with some third-party C codes. The compiled binaries are available for most operating systems, and is fully parallelized with OpenMP.

The name of the program “ABCluster” comes from an algorithm that developed in 2005, i.e. the artificial bee colony algorithm. This algorithm is inspired by the foraging behaviour of bee colonies in nature, by which the bees can find the “best” nectar sources. ABCluster mimics this, trying to find the geometry of a cluster with the lowest energy. Unlike some other ones, controlling the ABC algorithm needs only three parameters. This significantly lowers users’ study curve, enabling them to quickly get the geometrical information without adjusting parameters.

The author knows that many people are very reluctant to read lengthy and tedious manuals, thus the manual is kept as short as possible. There are only five chapters: Chapter 1 gives you an introduction to ABCluster; Chapter 2 gives a minimal description of the theory behind ABCluster; Chapter 3 and 4 tell you how to use ABCluster to treat atomic and rigid molecular clusters, respectively; Chapter 5 tells you how to use ABCluster and third-party programs (e.g. a quantum chemistry program) to perform the global optimization.

### 1.2 Contacting the Author

If you want to get the **source codes**, or have any bug reports, comments, suggestions or the possibility of cooperation on ABCluster, please feel free to contact to Dr. Jun Zhang by E-mail:

ZhangJunQcc@gmail.com

### 1.3 Program Citation

For any published works using ABCluster please include the following reference[1]:

Zhang, J.; Dolg, M. ABCluster: The Artificial Bee Colony Algorithm for Cluster Global Optimization. *Phys. Chem. Chem. Phys.* **2015**, *17*, 24173–24181.

If you apply ABCluster on molecular clusters, please also cite[2]:

Zhang, J.; Dolg, M. Global Optimization of Clusters of Rigid Molecules Using the Artificial Bee Colony Algorithm. *Phys. Chem. Chem. Phys.* **2016**, *18*, 3003–3010.

ABCluster is developed at Institute for Theoretical Chemistry, University of Cologne (in German: Institut für Theoretische Chemie, Universität zu Köln). The main author of ABCluster is Dr. Jun Zhang.

### 1.4 Copyright and Disclaimer

ABCluster is Copyright © 2015 Jun Zhang. ABCluster is free of charge to non-profit academic use. The use of ABCluster in commercial packages is not allowed without a prior written commercial license agreement.

The following codes used by ABCluster have special restrictions:

- `libLBFGS` (see <http://www.chokkan.org/software/liblbfgs>)

`libLBFGS` is the C realization of the limited-memory Broyden–Fletcher–Goldfarb–Shanno (L-BFGS) method[3]. It is Copyright © 2002-2014 Naoaki Okazaki. `libLBFGS` is distributed under the term of the MIT license.

- `Boost` (see <http://www.boost.org>)

`Boost` is a set of C++ libraries. It is Copyright © 2004-2006 Joe Coder. `Boost` is distributed under the Boost Software License, Version 1.0.

### 1.5 Components of ABCluster

When you download the ABCluster and unzip it, you can get several files:

- `atom-optimizer` The component to perform the global optimization of atomic cluster.
- `rigidmol-optimizer` The component to perform the global optimization of rigid molecular cluster.
- `isomer` The component to perform the global optimization of clusters in combination with third-party programs.
- `abcinp` The component to generate the input files for `atom-optimizer`.
- `xyz2gaussian` The component to combine ABCluster with Gaussian.
- `gaussian2xyz` The component to combine ABCluster with Gaussian.
- `bee` Now it can get some news of ABCluster via internet.
- `manual.pdf` The manual to ABCluster.
- `testfiles` This directory contains some test input files.

## 1.6 Installation of ABCluster

ABCluster does not need to be installed or configured! Please note that the current version of ABCluster does not have a graphic user interface (GUI). One must use it in the command line. You can use ABCluster by its absolute path every time, if you wish. You can also set “PATH” variable to the directory where ABCluster resides.

For Windows users: Assume you put ABCluster (`atom-optimizer.exe`, etc) in the directory `D:\ABCluster`, then open `Start`→`Control Panel`→`System or Security`→`System`, then click `Advanced System Settings`, choose the `Environment Variables` option. In the `System variables` list, choose `Path`, then click `Edit`. In the editbox, add “`;D:\ABCluster`” (Don’t forget the semicolon “`;`” !) at the end of the texts in it, and click `OK` to confirm it.

For Linux and Mac OS X users: ABCluster (`atom-optimizer`, etc) in the directory `/home/you/bin/abcluster`, then open your `.bashrc`. At the end of the file, add the statement “`export PATH=$PATH:/home/you/bin/abcluster`”, and run the command `source ~/.bashrc`.

Moreover, ABCluster is parallelized by OpenMP. In default it will use all the CPU cores of the machine on which it is run. If you want to change this behaviour, please set `OMP_NUM_THREADS` variable to the number of CPU cores you want to use.

Now ABCluster is ready, please enjoy it!



## Chapter 2

# Theory behind ABCluster

### 2.1 Choose Your Cluster and Potential Energy Function

Before using ABCluster to perform the global optimization of clusters, you should know what “type” of clusters and potential energy functions you need.

Given the geometry  $\mathbf{X}$  of a cluster, the potential energy function  $U(\mathbf{X})$  can describe its potential energy. In principle, it can be calculated by quantum chemical methods. However, a global optimization requires a large number of energy calculations. Using quantum chemistry is often too time-consuming. Moreover, except a few cases, many clusters can be described quite well by empirical potentials. These empirical potentials have been designed and optimized for specific purpose, and are much cheaper in computational cost than the first-principle ones. Therefore, we recommend that you use ABCluster and its built-in empirical potentials to do a **first** exploration for the clusters, then use quantum chemistry to study some important species found by ABCluster.

1. **Ionic clusters.** If you are studying clusters containing ions, like  $(\text{Na}^+\text{Cl}^-)_{30}$ ,  $(\text{Mg}^{2+}\text{O}^{2-})_{20}$ , you should use **Coulomb-Born-Mayer** potentials. See Equation 3.1.1.
2. **Large Metal and alloy clusters.** For the study of something like  $\text{Pt}_{38}$ ,  $\text{Ag}_{90}\text{Au}_{10}$ , **Gupta** or **Sutton–Chen** are the your choices. The former seems to be better since more parameters are available. See Equation (3.1.11) and (3.1.13). However, for **small** metallic clusters, like  $\text{Au}_8$ ,  $\text{Cu}_{10}$ , the two potentials are very inaccurate. One must use quantum chemistry methods to search their structures.
3. **Fullerene clusters.** The **Girifalco** potential is the most suitable one. See Equation (3.1.7). In this potential, the fullerene will be described as a point. If its explicit orientation is required, you will have to use **non-bonded potential**. See Equation (4.1.1).
4. **oxides, silicates, and silica-based glasses.** Use **Coulomb–Morse–Repulsion** potential. See Equation (3.1.5).
5. **Molecular clusters.** You will always use **non-bonded** potential. See Equation (4.1.1).
6. **Other model potentials.** ABCluster also supports some model potentials, like Morse potential. See Section (3.1).
7. For systems containing significant many-body effects, like inorganic or small metallic clusters (e.g.  $\text{Al}_3\text{O}_4^+$ ,  $\text{Au}_8$ ), it seems that only quantum chemistry can describe

it reasonably. ABCluster can combine with some quantum chemical software, e.g. Gaussian[4], ORCA[5], to compute the energies.

Once you confirm the system you need, you can choose the potentials listed above. The parameters of the potentials have to be searched from literatures, or fitted by yourself. Note that on ABCluster website, there will be a continuous updating of the parameters collected by the author. Thus if you need parameters for ABCluster, please check this website:

[http://www.uni-koeln.de/math-nat-fak/tcchem/mitarbeiter/  
zhang/zhang/software-abcluster-resources.html](http://www.uni-koeln.de/math-nat-fak/tcchem/mitarbeiter/zhang/zhang/software-abcluster-resources.html)

## 2.2 The Artificial Bee Colony Algorithm

ABCluster uses the so-called “artificial bee colony” (ABC) algorithm to perform the global optimization. It was proposed by Karaboga in 2005[6] and soon gains a lot of studies and applications in various problems. The ABC algorithm mimics the foraging behaviour of bees. ABCluster models this behaviour by three kinds of bees: employed bees (EM), onlooker bees (OL) and scout bees (SC). A colony tries to find the best nectar as food source. To do this, EMs perform a first search; OLs based on the knowledge of *all* EMs perform a further research; SCs have a memory of the previous search results and decide which nectars are of low quality and then discard them. After several cycles of search the colony can find the best nectar.

Now we interpret this model to the algorithm used in ABCluster. For the global optimization of chemical cluster geometry, a trial solution  $\mathbf{X}$  is the nectar and the smoothed potential energy  $U$  is its quality (a lower numeric value indicates a higher quality). The cluster is characterized by its size  $N$ , the estimated maximum coordinate value  $L$  (see Figure 2.2.1), and of course the potential parameters. The parameters needed for the ABC algorithm are the following: the size of the population of trial solutions  $SN$ , the scout limit  $g_{\text{limit}}$  and the maximum cycle number  $g_{\text{max}}$ . Here are some typical choices:

$SN$	10 to 300 or larger
$g_{\text{max}}$	100 to 100000 or larger
$g_{\text{limit}}$	3 to 10

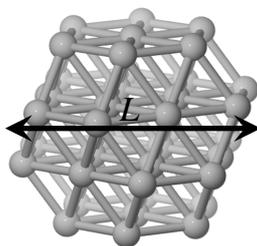


Figure 2.2.1: The graphic illustration of  $L$ .

For details of the algorithms used in ABCluster, please refer to ABCluster citation paper[1]. In the following chapters we will give some small systems as examples. In a real scientific research by ABCluster, you should **remember** the following tips:

- For large clusters, a better strategy is to perform **several optimizations with different initial guesses** and compare the final results.

- For clusters with **short-ranged or multimodal** interactions or with **multiple interaction sites** (like H<sub>2</sub>O which has two hydrogen bond acceptor and two donor sites), very large  $g_{\max}$  and  $SN$  are required to get reliable results, e.g. for some clusters with short-ranged Morse potential,  $g_{\max} = 15000$  and  $SN = 100$  are required.
- $L$  can be 1.5 to 3 times larger than system size.
- The parameters for atomic clusters can be obtained from literatures. For molecular clusters, one can construct its force field parameters from CHARMM, OPLS or AMBER. Remember the form of equation (4.1.1) and that **unit** of  $\epsilon$  and  $\sigma$  is kJ mol<sup>-1</sup> and Å, respectively! With wrong units you will get absurd results. Of course, one can design his own parameters. Please visit the ABCluster website for more information.
- When you get a lot of local minima, try to pick up the useful ones by **chemical intuition** and study them by quantum chemistry!

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## Chapter 3

# The Global Optimization of Atomic Clusters

### 3.1 Introduction

The atoms in an atomic cluster can interact with each by various kinds of potentials. Here “atom” can also mean “particle”, like an ion. ABCluster now support many kinds of potentials, including:

1. Coulomb–Born–Mayer potential[7]  $\text{CBM}_N$ . Very suitable for a description of ionic clusters.

$$U_{\text{CBM}} = \sum_{i=1}^N \sum_{i<j}^N \left( \frac{e^2}{4\pi\epsilon_0} \frac{q_i q_j}{r_{ij}} + B_{ij} \exp\left(-\frac{r_{ij}}{\rho_{ij}}\right) \right) \quad (3.1.1)$$

2. Lennard-Jones potential[8] ( $\text{LJ}_N$ ). Widely used to describe the dispersion interaction in chemistry.

$$U_{\text{LJ}} = \sum_{i=1}^N \sum_{i<j}^N 4\epsilon_{ij} \left( \left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}}\right)^6 \right) \quad (3.1.2)$$

3. Coulomb–Lennard-Jones potential ( $\text{CLJ}_N$ ). Includes both the Coulomb and dispersion interaction.

$$U_{\text{LJ}} = \sum_{i=1}^N \sum_{i<j}^N \left( \frac{q_i q_j}{r_{ij}} + 4\epsilon_{ij} \left( \left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}}\right)^6 \right) \right) \quad (3.1.3)$$

4. Morse potential[9] ( $\text{M}_N$ ). A more advanced form than the harmonic potential for the description of the vibration of molecules.

$$U_{\text{M}} = \sum_{i=1}^N \sum_{i<j}^N \epsilon_{ij} \left( \exp(-n\beta_{ij}(r_{ij} - r_{ij}^0)) - n \exp(-\beta_{ij}(r_{ij} - r_{ij}^0)) \right) \quad (3.1.4)$$

5. Coulomb–Morse–Repulsion potential[10] ( $\text{CMR}_N$ ). This is very useful in the simulation of oxides, silicates, and silica-based glasses.

$$U_{\text{CMR}} = \sum_{i=1}^N \sum_{i<j}^N \left( \frac{q_i q_j}{r_{ij}} + D_{ij} \left( \exp(-2\alpha_{ij}(r_{ij} - \rho_{ij})) + 2 \exp(-\alpha_{ij}(r_{ij} - \rho_{ij})) + \frac{C_{ij}}{r_{ij}^{12}} \right) \right) \quad (3.1.5)$$

6. Z potential[11] ( $Z_N$ ). This is inspired by an earlier potential proposed by Dzugutov[12, 13] which was designed to study glass formation. Unlike CBM, LJ and M potentials, they contain minima as well as maxima, which make the close-packing energetically unfavourable and lead to amorphous structures.

$$U_Z = \sum_{i=1}^N \sum_{i<j}^N \left( a \frac{e^{\alpha r_{ij}}}{r_{ij}^3} \cos(2k_F r_{ij}) + b \left( \frac{\sigma}{r_{ij}} \right)^m + V_0 \right) \theta(r_c - r_{ij}) \quad (3.1.6)$$

7. Girifalco[14] ( $Gf_N$ ). An effective potential of the fullerene-fullerene interaction.

$$U_{Gi} = \sum_{i=1}^N \sum_{i<j}^N \left( -\alpha \left( \frac{1}{s_{ij}(s_{ij}-1)^3} + \frac{1}{s_{ij}(s_{ij}+1)^3} - \frac{2}{s_{ij}^4} \right) + \beta \left( \frac{1}{s_{ij}(s_{ij}-1)^9} + \frac{1}{s_{ij}(s_{ij}+1)^9} - \frac{2}{s_{ij}^{10}} \right) \right) \quad (3.1.7)$$

$$s_{ij} = \frac{r_{ij}}{2d} \quad (3.1.8)$$

$$\alpha = \frac{N_C^2 A}{12(2d)^6} \quad (3.1.9)$$

$$\beta = \frac{N_C^2 B}{90(2d)^{12}} \quad (3.1.10)$$

8. Gupta potential[15] ( $G_N$ ). A very important many-body potential for modeling metals.

$$U_G = \sum_{i=1}^N \left( \sum_{\substack{j=1 \\ j \neq i}}^N A_{ij} \exp \left( -p_{ij} \left( \frac{r_{ij}}{d_{ij}} - 1 \right) \right) - \sqrt{\rho(\mathbf{r}_i)} \right) \quad (3.1.11)$$

where:

$$\rho(\mathbf{r}_i) = \sum_{\substack{j=1 \\ j \neq i}}^N \xi_{ij}^2 \exp \left( -2q_{ij} \left( \frac{r_{ij}}{d_{ij}} - 1 \right) \right) \quad (3.1.12)$$

9. Sutton–Chen potential[16] ( $SC_N$ ). Another many-body potential for modeling metals.

$$U_{SC} = \sum_{i=1}^N \left( \frac{1}{2} \sum_{\substack{j=1 \\ j \neq i}}^N \epsilon_{ij} \left( \frac{a_{ij}}{r_{ij}} \right)^p - \sqrt{\rho(\mathbf{r}_i)} \right) \quad (3.1.13)$$

where:

$$\rho(\mathbf{r}_i) = \sum_{\substack{j=1 \\ j \neq i}}^N c_{ij}^2 \left( \frac{a_{ij}}{r_{ij}} \right)^q \quad (3.1.14)$$

Now we will see how to perform global optimization on these clusters.

### 3.2 Example 1: 38 Lennard-Jones Particles

We have 38 particles interacting with Lennard-Jones potential (3.1.2), denoting as LJ<sub>38</sub>. We want to get its global minimum.

Step 1: In the ABCluster distribution, go to the directory `testfiles/atomiccluster`.

Step 2: Use `abcinp` to generate the input files:

```
../../../../abcinp lj38 1 LennardJones 5.0 30 300 5 30 38 C
Parameters for atom 0: sigma epsilon > 1.4 1.0
```

This line will be explained in the next section.

Step 3: Run the global optimization:

```
../../../../atom-optimizer lj38.inp > lj38.out
```

Below is everything you get after optimization:

- `lj38.out` The main output file.
- `lj38.xyz` The global minimum in XYZ format. It can be read by e.g. VMD, CYLView.
- `lj38.gjf` The global minimum in Gaussian input format. It can be read by e.g. GaussView.
- `lj38-LM` Contains the local minima, each one having two files in XYZ and Gaussian input format, respectively. They are sorted by energy-increasing order, e.g. `0.xyz` is lower in energy than `13.xyz`.
- `abcluster*.xyz/gjf` The file containing the current found global minimum during the running of `rigidmol-optimizer`. If `rigidmol-optimizer` crashes before normal termination, one can use this `abcluster*.xyz` to start a new optimization.

Now, you can check the final global minimal energy in `lj38.out`:

```
1      29      -170.78466518
2  * Final Global Minimal Energy:      -173.92842659
3  * The Global Minimum is saved as: [ lj38.(gjf/.xyz) ]
```

with the geometry in `lj38.xyz` (See Figure 3.2.1 ). Also, in the directory `lj38-LM`, there are 30 local minima for you.

### 3.3 About abcinp

Now we want to explain in detail how to generate the input files with `abcinp`. `abcinp` will print help information when run without any arguments:

```
abcinp
```

```
abcinp filename kind_of_atoms forcefield amplitude sn gmax glimit nsaves natoms1 symbol1
forcefield = LennardJones:          sigma epsilon
forcefield = CoulombLennardJones:   q sigma epsilon
forcefield = Morse:                 power epsilon beta r0
forcefield = CoulombBornMayer:      q B rho
forcefield = CoulombMorseRepulsion: q D alpha rho C
forcefield = Girifalco:             nC A B d
forcefield = Dzugutov:              a alpha kF b sigma m rC V0
forcefield = Gupta:                 A xi d p q
forcefield = SuttonChen:            p q epsilon a c
```

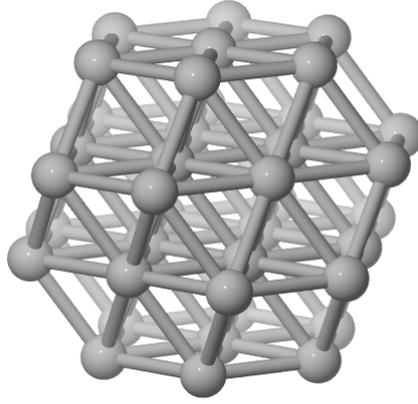


Figure 3.2.1: The global minimum of  $LJ_{38}$ .

We will interpret all the arguments:

- `filename` The unique filename. The generated input files will be named as “`filename.inp`”, “`filename.par`” and “`filenamei.xyz`”.
- `kind_of_atoms` The number of atomic types. For example, in the case of MgO clusters, `kind_of_atoms = 2`.
- `forcefield` The name of force field. Available choices are:
  - LennardJones, see (3.1.2).
  - CoulombLennardJones, see (3.1.3).
  - Morse, see (3.1.4).
  - CoulombBornMayer, see (3.1.1).
  - CoulombMorseRepulsion, see (3.1.5).
  - Girifalco, see (3.1.7).
  - Dzugutov, see (3.1.6).
  - Gupta, see (3.1.11) and (3.1.12).
  - SuttonChen, see (3.1.13) and (3.1.14).
- `amplitude` The estimated size of the cluster in Å, corresponding to “ $L$ ” mentioned in Section 2.
- `sn` The size of the population of trial solutions, corresponding to “ $SN$ ” mentioned in Section 2. Recommended value: 10 to 300.
- `gmax` The maximum cycle number, corresponding to “ $g_{\max}$ ” mentioned in Section 2. Recommended value: 100 to 100000 or larger.
- `glimit` The scout limit, corresponding to “ $g_{\text{limit}}$ ” mentioned in Section 2. Recommended value: 2 to 10.
- `nasves` The number of local minima to be saved.
- `natoms1 symbol1 ...` For all `kind_of_atoms` atoms, its number and symbol must be given. Here the “symbol” is not necessarily an element symbol like “C” or “Mg”, but can be any strings, like “CT2”.

After this the program will require you to input force field parameters for different pairs of atoms. The parameters are exactly the ones used from (3.1.1) to (3.1.14) in Section 3.1.

Now we give explicit correspondence between the variables in the program input and the potential expression:

Lennard-Jones, (3.1.2)	sigma - $\sigma$ ; epsilon - $\epsilon$
Coulomb–Lennard-Jones, (3.1.3)	q - $q$ ; sigma - $\sigma$ ; epsilon - $\epsilon$
Morse, (3.1.4)	power - $n$ ; epsilon - $\epsilon$ ; beta - $\beta$ ; r0 - $r^0$
Coulomb–Born–Mayer, (3.1.1)	q - $q$ ; B - $B$ ; rho - $\rho$
Coulomb–Morse–Repulsion, (3.1.5).	q - $q$ ; D - $D$ ; alpha - $\alpha$ ; rho - $\rho$ ; C - $C$
Girifalco, (3.1.7)	nC - $N_C$ ; A - $A$ ; B - $B$ ; d - $d$ ;
Dzugutov, (3.1.6)	a - $a$ ; alpha - $\alpha$ ; kF - $k_F$ ; b - $b$ ; sigma - $\sigma$ ; m - $m$ ; rC - $r_C$ ; V0 - $V_0$
Gupta, (3.1.11)	A - $A$ ; xi - $\xi$ ; d - $d$ ; p - $p$ ; q - $q$
SuttonChen, (3.1.13)	p - $p$ ; q - $q$ ; epsilon - $\epsilon$ ; a - $a$ ; c - $c$

For instance, in the last section, we use the following command:

```
../../abcpnp lj38 1 LennardJones 5.0 30 300 5 30 38 C
Parameters for atom 0: sigma epsilon > 1.4 1.0
```

This means: Perform a global optimization on a LennardJones cluster, with  $L = 5.0$ ,  $SN = 30$ ,  $g_{\max} = 300$ ,  $g_{\text{limit}} = 5$ , 30 local minima will be saved. We have 1 kind of particles, its number and symbol is 38 and C, respectively. The generated file will be named as lj38\*.

After this, you will get three files:

- lj38.inp The main input file.
- lj38.par The parameter file.
- lj38i.xyz Initial guess in XYZ format.

Open lj38.inp you will find this:

```

1 38          # number of atoms
2 lj38i.xyz   # initial guess file; * - random guess
3 LennardJones # force field types
4 lj38.par    # force field parametetrs
5 30          # population size
6 300        # maximal generations
7 5          # scout limit
8 5.00000000 # amplitude
9 lj38      # save optimized configuration to .xyz and .gjf
10 30       # number of LMs to be saved
```

This file can of course be modified manually. Especially, if you do not have an initial guess file, you can change Line 2 to a star \*, then ABCluster will automatically generate an initial guess.

### 3.4 Example 2: $(Mg^{Q+}O^{Q-})_{20}$

In this section we will find that the parameters can change the global minima significantly. We consider  $(MgO)_{20}$ . It can be described by Coulomb–Born–Mayer potential 3.1.1. A set of parameters is[17]:

---


$$\begin{aligned}
 &B(\text{Mg} - \text{O}) = 821.6; B(\text{Mg} - \text{Mg}) = 0.0; B(\text{O} - \text{O}) = 22764 \\
 &\rho(\text{Mg} - \text{O}) = 0.3242; \rho(\text{Mg} - \text{Mg}) = 0.1; \rho(\text{O} - \text{O}) = 0.1490 \\
 &q_{\text{Mg}} = +2.0; q_{\text{O}} = -2.0
 \end{aligned}$$


---

If we use  $L = 5.0$ ,  $SN = 100$ ,  $g_{\max} = 100$ ,  $g_{\text{limit}} = 5$ , then we can perform the global optimization:

```

../../abcpinp mg20o20-q2 2 CoulombBornMayer 5.0 100 100 5 30 20 Mg 20 0
Parameters for atom 0: q > +2
Parameters for atom 1: q > -2
Parameters for atom-pair 0-0: B rho > 0.0 0.1
Parameters for atom-pair 0-1: B rho > 821.6 0.3242
Parameters for atom-pair 1-1: B rho > 22746 0.1490

```

Since we have 2 kinds of atoms, “Mg” and “O”, we have to write 20 Mg 20 0 to indicate that we have 20 Mg and 20 O atoms. Now perform the optimization:

```
atom-optimizer mg20o20-q2.inp > mg20o20-q2.out
```

Before looking at its geometry, what will it be if the formal charge  $Q$  on Mg and O are not 2.0, but other numbers, e.g. 1.5 and 1.0? Let’s try it. Generate the input files for  $\text{Mg}^{1.5+}\text{O}^{1.5-}$

```

../../abcpinp mg20o20-q1.5 2 CoulombBornMayer 5.0 100 100 5 30 20 Mg 20 0
Parameters for atom 0: q > +1.5
Parameters for atom 1: q > -1.5
Parameters for atom-pair 0-0: B rho > 0.0 0.1
Parameters for atom-pair 0-1: B rho > 821.6 0.3242
Parameters for atom-pair 1-1: B rho > 22746 0.1490

```

and for  $\text{Mg}^{1.0+}\text{O}^{1.0-}$

```

../../abcpinp mg20o20-q1 2 CoulombBornMayer 5.0 100 100 5 30 20 Mg 20 0
Parameters for atom 0: q > +1.0
Parameters for atom 1: q > -1.0
Parameters for atom-pair 0-0: B rho > 0.0 0.1
Parameters for atom-pair 0-1: B rho > 821.6 0.3242
Parameters for atom-pair 1-1: B rho > 22746 0.1490

```

Run them!

```

atom-optimizer mg20o20-q1.5.inp > mg20o20-q1.5.out
atom-optimizer mg20o20-q1.inp > mg20o20-q1.out

```

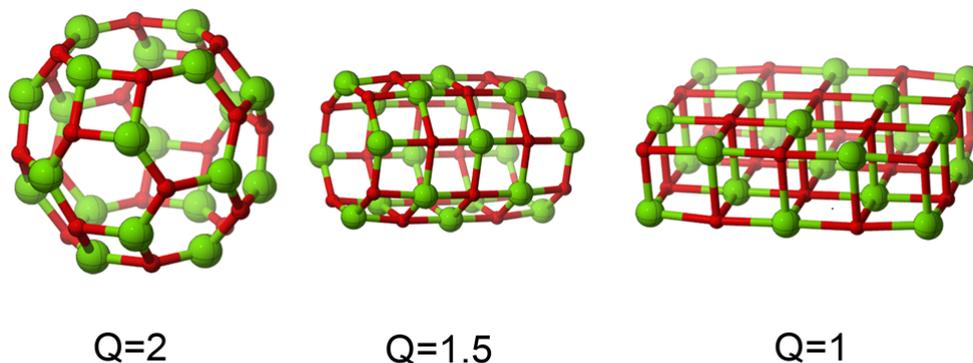
Now check `mg20o20-q2.xyz`, `mg20o20-q1.5.xyz` and `mg20o20-q1.xyz`, you will observe that the global minimum is a sphere, tube and cuboid, respectively!

## 3.5 Example 3: Silver and Copper Clusters

### 3.5.1 $\text{Ag}_{38}$ and $\text{Cu}_{38}$

Assuming you get a silver and copper cluster. By mass spectroscopy you know that their formulae are  $\text{Ag}_{38}$  and  $\text{Cu}_{38}$ , respectively. What are their most stable structures?

The best potential for metal clusters are Gupta potential (3.1.11). From the literature[18], one can find their Gupta potential parameters:

Figure 3.4.1: The global minimum of  $(\text{MgO})_{20}$ .

	$A$	$\xi$	$d$	$p$	$q$
Ag-Ag	0.1028	1.1780	2.8885	10.928	3.1390
Cu-Cu	0.0855	1.2240	2.5562	10.960	2.2780
Cu-Ag	0.0980	1.2274	2.7224	10.700	2.8050

OK, now we can perform the global optimization. Let's see  $\text{Ag}_{38}$  first.

Step 1: Use `abcpnp` to generate the input files:

```
abcpnp Ag38 1 Gupta 10 100 100 5 20 38 Ag
Parameters for atom-pair 0-0: A xi d p q > 0.1028 1.1780 2.8885 10.928 3.1390
```

Step 2: Run the optimization:

```
nohup atom-optimizer Ag38.inp > Ag38.out &
```

Step 3: Now we examine the structure by opening the file `Ag38.xyz`. See Figure 3.5.1.

Now we do the same for  $\text{Cu}_{38}$ .

Step 1: Use `abcpnp` to generate the input files:

```
abcpnp Cu38 1 Gupta 10 100 100 5 20 38 Cu
Parameters for atom-pair 0-0: A xi d p q > 0.0855 1.2240 2.5562 10.960 2.2780
```

Step 2: Run the optimization:

```
nohup atom-optimizer Cu38.inp > Cu38.out &
```

Step 3: Now we examine the structure by opening the file `Ag38.xyz`. See Figure 3.5.1.

Interestingly, both are a truncated octahedron.

### 3.5.2 $\text{Ag}_{32}\text{Cu}_6$

However, you may get a “nanoalloy”, a mixture of silver and copper atoms. For example, the alloy is  $\text{Ag}_{32}\text{Cu}_6$ . What shape will it be? Still truncated octahedron? Let's see.

Step 1: Use `abcpnp` to generate the input files:

```
abcpnp Ag32Cu6 2 Gupta 10 3000 5000 5 20 32 Ag 6 Cu
Parameters for atom-pair 0-0: A xi d p q > 0.1028 1.1780 2.8885 10.928 3.1390
Parameters for atom-pair 0-1: A xi d p q > 0.0980 1.2274 2.7224 10.700 2.8050
Parameters for atom-pair 1-1: A xi d p q > 0.0855 1.2240 2.5562 10.960 2.2780
```

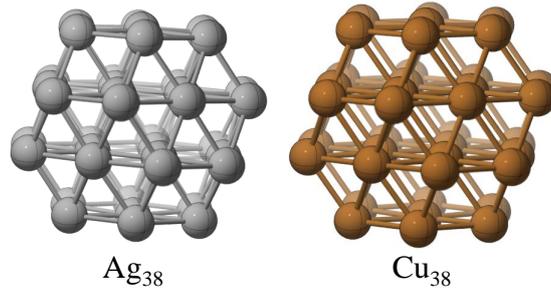


Figure 3.5.1: The global minimum of Ag<sub>38</sub> and Cu<sub>38</sub>.

Note that, for mixed alloys, the number of steps required to find the global minimum may be very large. In ABCluster 1.1 or 1.2 we have to set very large  $SN$  and  $g_{\max}$ , see examples files in `Ag32Cu6-slow-1.1` where  $SN = 3000$  and  $g_{\max} = 5000!$ . Fortunately, from ABCluster 1.3, we improved the algorithm significantly and now moderately parameters works quiet well! Try to set  $SN = 300$  and  $g_{\max} = 300$ . During the running you can examine the current global minimum by examining the temporal file `abcluster*.xyz`.

Step 2: Run the optimization:

```
nohup atom-optimizer Ag32Cu6.inp > Ag32Cu6.out &
```

Step 3: Now we examine the structure by opening the file `Ag32Cu6.xyz`. See Figure 3.5.2. Amazingly, it is not a “pancake”, with the six copper atoms forming a hexagonal ring!

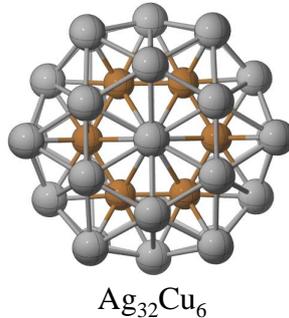


Figure 3.5.2: The global minimum of Ag<sub>32</sub>Cu<sub>6</sub>.

### 3.6 Example 4: Perovskite Clusters (CaTiO<sub>3</sub>)<sub>5</sub>

Perovskite recently attracts much attention from its scientific community due to its unexpected application in solar cells. Assum now you want to know the structure of (CaTiO<sub>3</sub>)<sub>5</sub>, you can do this job by ABCluster. For such systems, the so-called Coulomb–Morse–Repulsion potential (3.1.5) can be used. One can get the interaction parameter Ca–O, Ti–O and O–O from Ref. [10]. For cation interaction Ca–Ca and Ti–Ti, only the Coulomb term ( $1/r$ ) and strong repulsion term ( $1/r^{12}$ ) are considered (Assume  $C = 22$ ), the Morse term can be assumed to be zero (thus  $D$ ,  $\alpha$  and  $\rho$  are all zero). The final parameters are:

	$q(\text{Ca}) = +1.2$	$q(\text{Ti}) = +2.4$	$q(\text{O}) = -1.2$	
	$D$	$\alpha$	$\rho$	$C$
Ca-Ca	0	0	0	22.0
Ca-Ti	0	0	0	22.0
Ca-O	0.030211	2.241334	2.923245	5.0
Ti-Ti	0	0	0	22.0
Ti-O	0.024235	2.254703	2.708943	1.0
O-O	0.042395	1.379316	3.618701	22.0

Now the optimization starts.

Step 1: Use `abcinp` to generate the input files:

```

abcinp catio3 3 CoulombMorseRepulsion 10 100 1000 5 10 5 Ca 5 Ti 15 0
Parameters for atom 0: q > +1.2
Parameters for atom 1: q > +2.4
Parameters for atom 2: q > -1.2
Parameters for atom-pair 0-0: D alpha rho C > 0 0 0 22.0
Parameters for atom-pair 0-1: D alpha rho C > 0 0 0 22.0
Parameters for atom-pair 0-2: D alpha rho C > 0.030211 2.241334 2.923245 5.0
Parameters for atom-pair 1-1: D alpha rho C > 0 0 0 22.0
Parameters for atom-pair 1-2: D alpha rho C > 0.024235 2.254703 2.708943 1.0
Parameters for atom-pair 2-2: D alpha rho C > 0.042395 1.379316 3.618701 22.0

```

Step 2: Run the optimization:

```
nohup atom-optimizer catio3.inp > catio3.out &
```

Step 3: Now we examine the structure by opening the file `catio3.xyz`. See Figure 3.6.1. Note that it is very different from a bulk, perovskite crystal structure.

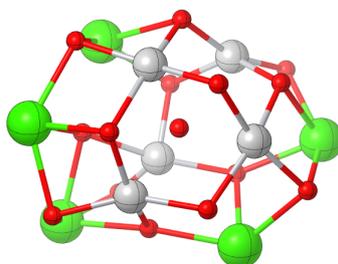


Figure 3.6.1: The global minimum of  $(\text{CaTiO}_3)_5$ .



## Chapter 4

# The Global Optimization of Rigid Molecular Clusters

### 4.1 Introduction

Molecular clusters are very important in several field of chemistry, biology and physics. In the current version of ABCluster, the molecules in cluster are assumed to be **rigid**, meaning that the internal degrees of freedoms (bond lengths, bond angles, dihedral angles, etc.) are kept unchanged during the optimization. For small molecules this is a very good approximation. Thus each molecule in the cluster can be described by six external degrees of freedoms: the coordinates of its geometrical center  $\mathbf{R} \equiv \{X, Y, Z\}$  and three Euler angles  $\Omega \equiv \{\alpha, \beta, \gamma\}$  relative to its pre-defined body-fixed coordinate system.

The potential energy of the rigid molecular cluster is assumed to be of the following form:

$$U(\mathbf{Q}) = \sum_{I=1}^N \sum_{I < J}^N \sum_{i_I \in I} \sum_{j_J \in J} \left( \frac{e^2}{4\pi\epsilon_0} \frac{q_{i_I} q_{j_J}}{r_{i_I j_J}} + 4\epsilon_{i_I j_J} \left( \left( \frac{\sigma_{i_I j_J}}{r_{i_I j_J}} \right)^{12} - \left( \frac{\sigma_{i_I j_J}}{r_{i_I j_J}} \right)^6 \right) \right) \quad (4.1.1)$$

Obviously, (4.1.1) describes the intermolecular Coulomb and Lennard-Jones interactions. This simple form enables one to compute large systems fast and quickly gain chemical insights. **One can get a lot of local minima by ABCluster first, and then use high-level theory, like quantum chemistry, to further study these isomers.**

The unit of  $\epsilon$  and  $\sigma$  in (4.1.1) is  $\text{kJ mol}^{-1}$  and  $\text{\AA}$ , respectively. These parameters can be obtained from modern force fields, like CHARMM[19], OPLS[20] and AMBER[21]. Some molecule files suitable for ABCluster are available in the distribution in

```
testfiles/rigidmolecularcluster/charmm36
testfiles/rigidmolecularcluster/oplsaa
```

Also, the latest force field parameters will be available on the ABCluster website.

### 4.2 Example 1: $(\text{H}_2\text{O})_6$

We want to know the most stable structure of  $(\text{H}_2\text{O})_6$ . We describe water by TIP4P model. This can be done in the following steps.

Step 1: In the ABCcluster distribution, go to the directory `testfiles/rigidmolecularcluster`. Note that there is a directory `charmm36`.

Step 2: Prepare an input file named `h2o6.inp` with the following content:

```

1 input.cluster      # cluster file name
2 20                 # population size
3 20                 # maximal generations
4 3                  # scout limit
5 4.000000000       # amplitude
6 h2o6               # save optimized configuration
7 30                 # number of LMs to be saved

```

This file is self-explained:

- Line 1: The name of the file that contains the cluster components and geometry, it will be explained in the next step.
- Line 2: The size of the population of trial solutions, corresponding to “ $SN$ ” mentioned in Section 2. The larger the cluster, the larger  $SN$  is required.
- Line 3: The maximum cycle number, corresponding to “ $g_{\max}$ ” mentioned in Section 2. For such small systems 20 is sufficient. For larger ones, perhaps 100000 is required!
- Line 4: The scout limit, corresponding to “ $g_{\text{limit}}$ ” mentioned in Section 2. Usually 3 to 10 is OK.
- Line 5: The estimated size of the cluster in Å, corresponding to “ $L$ ” mentioned in Section 2. For an efficient optimization of large systems, this value should be 1.5 to 3 times of the system size.
- Line 6: The name to save the results.
- Line 7: The number of local minima to be saved.

Step 3: Prepare the cluster file named `input.cluster` with the following content:

```

1 1
2 charmm36/tip4p.xyz      6
3 * 4.0000

```

Here:

- Line 1: The number of different components in the cluster. For  $(\text{H}_2\text{O})_6$  this is 1. For  $\text{Na}^+(\text{H}_2\text{O})_3(\text{CH}_3\text{OH})_2$ , this is 3.
- Line 2: The file name (with path!) containing the coordinates and force field parameters, and the number of this molecules in the cluster. If there are more than one components in the cluster, then each component should be described by a line like this.
- Line 3: Here, “\* 4.0000” means generating a random initial guess with  $L = 4.0000$

It can also have another form:

```

1 1
2 charmm36/tip4p.xyz 6
3 Water hexamer
4 3.5 7.0 -0.2 1.3 2.9 0.6
5 4.0 0.9 3.1 4.3 3.2 3.8
6 -1.8 4.4 1.0 0.8 0.2 0.6
7 4.2 3.4 3.9 1.9 0.2 3.2
8 3.6 4.7 2.9 3.6 1.7 1.7
9 5.1 5.2 -0.6 1.6 2.8 3.5

```

In ABCluster, as long as the first line after cluster components is not of the form like “\* 5.000” but anything else (e.g. a title), then in the following one has to give an explicit initial guess in the form  $X, Y, Z, \alpha, \beta$  and  $\gamma$ .

Step 4: Now we have `h2o6.inp` and `input.cluster`, we can run the global optimization:

```
../../rigidmol-optimizer h2o6.inp > h2o6.out
```

When the optimization is finished, we get the following files.

- `h2o6.out` The main output file.
- `h2o6-0PT.xyz` The global minimum in XYZ format. It can be read by e.g. VMD, CYLView.
- `h2o6-0PT.gjf` The global minimum in Gaussian input format. It can be read by e.g. GaussView.
- `h2o6-0PT.cluster` The global minimum in ABCluster format. It can only be read by rigidmol-optimizer. Also, it can be used as the initial guess of a new optimization.
- `h2o6-LM` Contains the local minima, each one having three files in XYZ, Gaussian input, and ABCluster format. They are sorted by energy-increasing order, e.g. `0.xyz` is lower in energy than `13.xyz`.
- `abcluster*.xyz/gjf/cluster` The file containing the current found global minimum during the running of rigidmol-optimizer. If rigidmol-optimizer crashes before normal termination, one can use this `*.cluster` to start a new optimization.

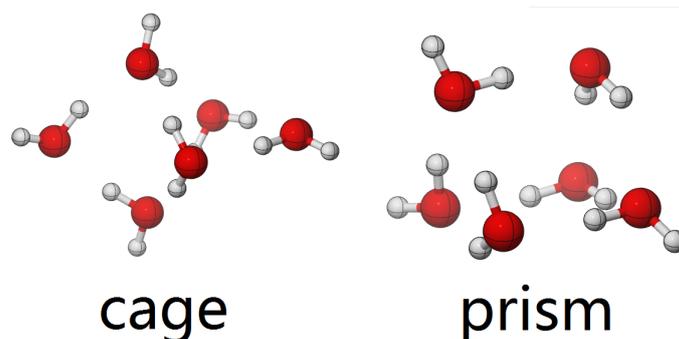
Now let us see the result. The `h2o6.out` is similar to that generated by atom-optimizer, thus will not be explained again here. Open `h2o6-0PT.xyz`, we found that the global minimum is the cage isomer. Open `h2o6-LM/2.xyz`, we found a local minimum: the prism isomer. See Figure 4.2.1. To get a reliable conclusion on which one is more stable, please use high-level methods like quantum chemistry for further study. Of course, we can play with all 30 local minima!

### 4.3 Example 2: $Li^+$ , $Na^+$ and $Cs^+$ in $(C_6H_6)_6$

The section title gives three cation- $\pi$  system. Let’s see what its global minimum will be.

Step 1: In the ABCluster distribution, go to the directory `testfiles/rigidmolecularcluster`. Note that there is a directory `charmm36`.

Step 2: Optimize  $Li^+(C_6H_6)_6$ . Prepare two files: `li-ben.inp` and `li-ben.cluster`:

Figure 4.2.1: The two minima of  $(\text{H}_2\text{O})_6$ .

```

1 li-ben.cluster # cluster file name
2 20             # population size
3 20            # maximal generations
4 3             # scout limit
5 10.00000000   # amplitude
6 li-ben        # save optimized configuration
7 30            # number of LMs to be saved

```

```

1 2
2 charmm36/c6h6.xyz      6
3 charmm36/li.xyz       1
4 * 10.0000

```

Then run the optimization:

```
../../rigidmol-optimizer li-ben.inp > li-ben.out
```

Step 3: Do the similar thing for  $\text{Na}^+(\text{C}_6\text{H}_6)_6$  and  $\text{Cs}^+(\text{C}_6\text{H}_6)_6$ . Remember to change the file name from `li*` to `na*` or `cs*`, and in `*.cluster`, change `charmm36/li.xyz` to `charmm36/na.xyz` or `charmm36/cs.xyz`.

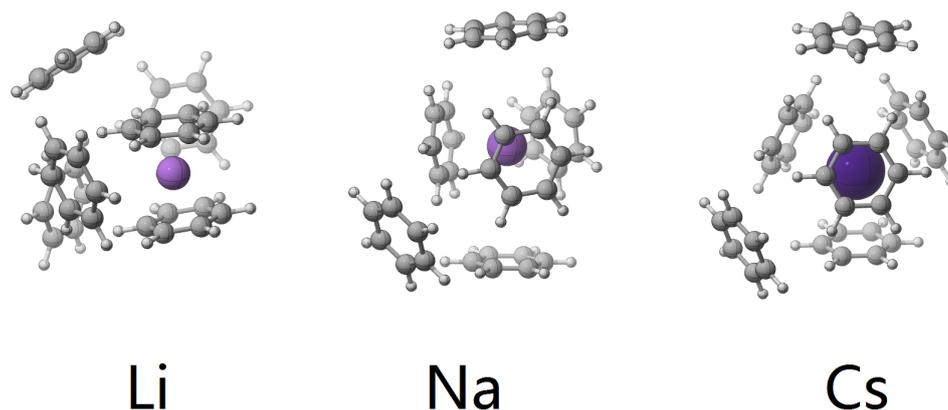
Now let's open `li-ben-OPT.xyz`, `na-ben-OPT.xyz` and `cs-ben-OPT.xyz` to see their global minima, shown in Figure 4.3.1.

One can see that in the first solvation shell,  $\text{Li}^+$  has only 2  $\text{C}_6\text{H}_6$ , but  $\text{Na}^+$  and  $\text{Cs}^+$  have 5. Moreover, the remaining  $\text{C}_6\text{H}_6$  is more closer to  $\text{Cs}^+$  than that to  $\text{Na}^+$ . This is obviously related to their charge density. Maybe you want to see what will happen for  $\text{K}^+$  or  $\text{SO}_4^{2-}$ . Just try it! ABCluster can do many amazing things!

#### 4.4 Example 3: $(\text{CH}_2=\text{CH}_2)_{13}$

Ethene is of fundamental importance in chemical industrial. Now we want to know the global minimum of  $(\text{CH}_2=\text{CH}_2)_{13}$ . However, it seems that there is no ethene in `testfiles/rigidmolecularcluster/charmm36`. Therefore we have to construct it by ourselves.

Step 1: Construct the geometry of  $\text{CH}_2=\text{CH}_2$ . An optimization at B3LYP/6-31G(d) level is sufficient for our purpose. The final geometry is stored in a file named `c2h4.xyz` in XYZ format:

Figure 4.3.1: The global minima of  $Li^+(C_6H_6)_6$ ,  $Na^+(C_6H_6)_6$  and  $Cs^+(C_6H_6)_6$ .

1	6				
2	ethene				
3	C	0.00000000	0.00000000	0.66542300	
4	H	0.00000000	0.92366200	1.23955100	
5	H	0.00000000	-0.92366200	1.23955100	
6	C	0.00000000	0.00000000	-0.66542300	
7	H	0.00000000	-0.92366200	-1.23955100	
8	H	0.00000000	0.92366200	-1.23955100	

Step 2: Construct the force field parameters of  $CH_2=CH_2$ . Since in this manual we always use CHARMM force field, for consistency we also use this for ethene. You can get the latest CHARMM force field files from:

<http://mackerell.umaryland.edu/charmm.ff.shtml>

At the time this manual is written, the latest version is CHARMM36. After you download `toppar_c36_aug14.tgz` and unzip it, fortunately there are parameters for ethene.

In the file `toppar/top_all36_cgenff.rtf` you find the following words :

1	RESI	ETHE	0.00	!	C2H4	ethylene,	yin/adm	jr.	
2	GROUP								
3	ATOM	C1	CG2D2	-0.42	!				
4	ATOM	H11	HGA5	0.21	!	H11	H21		
5	ATOM	H12	HGA5	0.21	!	\	/		
6	GROUP				!	C1=C2			
7	ATOM	C2	CG2D2	-0.42	!	/	\		
8	ATOM	H21	HGA5	0.21	!	H12	H22		
9	ATOM	H22	HGA5	0.21	!				
10	BOND	C1	H11	C1	H12				
11	DOUBLE	C1	C2						
12	BOND	C2	H21	C2	H22				
13	IC	H11	C1	C2	H21	1.1036	121.37	180.00	121.37 1.1036
14	IC	H12	C2	*C1	H11	1.1036	121.37	180.00	121.37 1.1036
15	IC	H22	C1	*C2	H21	1.1036	121.37	180.00	121.37 1.1036

```

16 IC C1 C2 H21 H22 1.3370 121.37 -180.00 31.37 1.8845
17 PATC FIRS NONE LAST NONE

```

Take the first line ATOM C1 CG2D2 -0.42 as example, C1 indicates the corresponding atom; CG2D2 is the atomic type; -0.42 is its  $q$  parameter in (4.1.1).

To find its  $\epsilon$  and  $\sigma$  parameters, we check the file `toppar/par_all136_cgenff.rtf`, and find this:

```

1 CG2D2 0.0 -0.0640 2.0800 ! alkene, yin, adm jr., 12/95

```

-0.0640 and 2.0800 are  $\epsilon$  and  $\sigma$ , respectively. However, since CHARMM and ABCluster use different formulae, we have to **transform** them! The transformation formulae is:

$$\epsilon_{\text{ABCluster}} = \epsilon_{\text{CHARMM}} \times (-4.184) \quad (4.4.1)$$

$$\sigma_{\text{ABCluster}} = \sigma_{\text{CHARMM}} \times 2^{\frac{5}{6}} \quad (4.4.2)$$

Thus its final value is:

$$q = -0.42 \quad (4.4.3)$$

$$\epsilon = -0.0640 \times (-4.184) = 0.2678 \quad (4.4.4)$$

$$\sigma = 2.0800 \times 2^{\frac{5}{6}} = 3.7061 \quad (4.4.5)$$

The parameters of H can be found in a similar way:

$$q = +0.21 \quad (4.4.6)$$

$$\epsilon = -0.0260 \times (-4.184) = 0.1088 \quad (4.4.7)$$

$$\sigma = 1.2600 \times 2^{\frac{5}{6}} = 2.2451 \quad (4.4.8)$$

Thus the final parameter file `c2h4.xyz` for  $\text{CH}_2=\text{CH}_2$  is:

```

1 6
2 ethene
3 C 0.00000000 0.00000000 0.66542300
4 H 0.00000000 0.92366200 1.23955100
5 H 0.00000000 -0.92366200 1.23955100
6 C 0.00000000 0.00000000 -0.66542300
7 H 0.00000000 -0.92366200 -1.23955100
8 H 0.00000000 0.92366200 -1.23955100
9 q epsilon (kJ/mol) sigma (AA)
10 -0.42 0.2678 3.7061 # CG2D2
11 +0.21 0.1088 2.2451 # HGA5
12 +0.21 0.1088 2.2451 # HGA5
13 -0.42 0.2678 3.7061 # CG2D2
14 +0.21 0.1088 2.2451 # HGA5
15 +0.21 0.1088 2.2451 # HGA5

```

Note that there is a comment line between the geometry and parameter section. The words after # are comments.

Step 3: Now prepare the files `c2h413.inp` and `input.cluster`:

```

1 input.cluster # cluster file name
2 20 # population size
3 100 # maximal generations
4 3 # scout limit

```

```

5 | 10.00000000    # amplitude
6 | c2h413        # save optimized configuration
7 | 30            # number of LMs to be saved

```

```

1 | 1
2 | c2h4.xyz      13
3 | * 10.0000

```

Please pay attention that in this case,  $g_{\max}$  should be larger than 100 to converge.  
Step 4: Run the global optimization:

```
../././rigidmol-optimizer c2h413.inp > c2h413.out
```

Now open *c2h413.out*, you can find something like this:

```

1 |      1      2.04470195    -126.16552671    -133.24995529    ...
2 |      2      2.92567497    -126.24112753    -138.25196792    ...
3 |      3      3.50028571    -126.84189306    -138.36356518    ...
4 |      4      3.41023240    -128.06552411    -138.36356515    ...
5 |      5      3.86775258    -126.57913695    -139.41470519    ...
6 |      6      5.85200692    -116.01432862    -140.13516658    ...
7 |      7      5.03267295    -124.05305628    -140.13516658    ...
8 |      .....
9 |     52      4.65923457    -120.62871046    -140.72175322    ...
10 |     53      3.74502721    -123.42238555    -140.72175322    ...
11 |     54      4.87904478    -120.29869548    -140.72175322    ...
12 |     55      4.73791669    -120.80626616    -140.72175322    ...
13 |     56      4.58123341    -124.32091734    -140.82027375    ...
14 |     57      5.84959151    -123.90112274    -140.82027371    ...
15 |     58      7.10242950    -122.13716432    -140.82027374    ...
16 |     .....
17 |     * Final Global Minimal Energy:    -140.82027375

```

At 56th step the final global minimal energy is located. The final global minimum has  $C_i$  symmetry (in Figure 4.4.1):

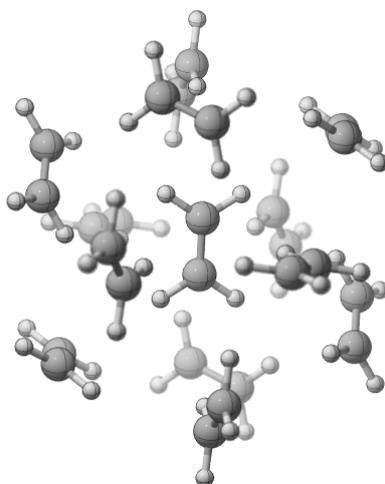


Figure 4.4.1: The global minimum of  $(CH_2=CH_2)_{13}$ .



## Chapter 5

# The Global Optimization with Third-party Programs

### 5.1 Introduction

In the last two chapters, we discussed several kinds of force fields which is supported natively by ABCluster. However, for species which exhibits strong many-body effects, like inorganic clusters or small metal clusters, to the best of the author's knowledge, no force fields can describe them reasonably. In these cases, one must use quantum chemistry instead of additive empirical force field potentials to calculate their energies. The component `isomer` of ABCluster is designed for this purpose. The program itself provides some simple interfaces. By using these interfaces one can perform the global optimization with energy calculated by **any** third-party programs, e.g. Gaussian, Gamess, VASP. Since these calculations are much more expensive than those of force fields, the ABC algorithm is simplified to increase the efficiency. We will now show how to combine the power of ABCluster and other programs.

### 5.2 ABCluster with Gaussian

Gaussian is one of the most popular quantum chemistry software, thus we have provided official support for it. In the distribution of ABCluster you can find two files: `xyz2gaussian` and `gaussian2xyz`. They will be used by ABCluster to compute the energy with Gaussian.

#### 5.2.1 Configuration of Gaussian

One must do some preparations before using Gaussian, e.g., setting up some environmental variables. If you have done this you can skip this section.

For Windows users: Assume you use Gaussian09 and put it in the directory `D:\G09W`, then open `Start`→`Control Panel`→`System` or `Security`→`System`, then click `Advanced System Settings`, choose the `Environment Variables` option. In the `User variables for you` list, click `New`. In the `Variable name` editbox, write `"GAUSS_EXEDIR"`, and in the `Variable value` editbox, write `"D:\G09W"`. Then click `OK` to confirm it.

For Linux and Mac OS X users: Assume you use Gaussian09 and put it in the directory `/home/you/g09` and you set the scratch directory for the computation as `/scratch/you`. then open your `.bashrc`. At the end of the file, add the statements:

```
export g09root="/home/you/g09"
export GAUSS_SCRDIR=/scratch/you
```

```
source $g09root/g09/bsd/g09.profile
```

### 5.2.2 Example: $\text{Al}_3\text{O}_4^+$

The first example is, what is the global minimum of the cluster  $\text{Al}_3\text{O}_4^+$ ? We decide to use a classical method: B3LYP/6-31g(d) to calculate energy. Now we will do this global optimization.

Step 1: In the ABCluster distribution, go to the directory `testfiles/qc`. Create a file called `mol.inp`. For Windows users, the content should be:

```

1 mol                # Result file name
2 Al 3 0 4          # Symbols
3 cube 3 3 3       # Structure types
4 30                # Maximal number of calculations
5 >>>>
6 ../../xyz2gaussian optfile $inp$ > $xxx$.gjf
7 "D:\G09W\g09.exe" $xxx$.gjf
8 ../../gaussian2xyz $xxx$.out > $out$
9 >>>>
```

For Linux and Mac OS X users,

```

1 mol                # Result file name
2 Al 3 0 4          # Symbols
3 cube 3 3 3       # Structure types
4 30                # Maximal number of calculations
5 >>>>
6 ../../xyz2gaussian optfile $inp$ > $xxx$.gjf
7 g09 < $xxx$.gjf > $xxx$.log 2>/dev/null
8 ../../gaussian2xyz $xxx$.log > $out$
9 >>>>
```

The meaning of each line is:

- Line 1: The name of the directory that stores the found local minima (LM). After optimization, all the found LMs will be stored in `mol-LM`.
- Line 2: The cluster components. For  $\text{Al}_3\text{O}_4^+$ , just write `Al 3 0 4`. For  $\text{Au}_{13}\text{Pt}_1$ , write `Au 13 Pt 1`.
- Line 3: For this line, one can give the type of initial guesses. Available choices are:
  - line Generate a linear initial structure.
  - ring Generate a ring initial structure.
  - sphere Generate a sphere initial structure.
  - plane 2 3 Generate a 2D initial structure from a  $2 \times 3$  lattice.
  - cube 3 4 3 Generate a 3D initial structure from a  $3 \times 4 \times 3$  lattice.

Note that this does **not** mean that the program will only give linear structures when you use line. It is just a “preference”.

- Line 4: The maximal number of calculations you want to do. Here it means `isomer` will do 30 calculations.

- The lines between two >>>> are the commands to call third-party programs to calculate the energy. This will be explained latter.

Step 2: Create a file named `optfile` with the following content:

```

1 %nproc=20
2 %mem=300GB
3 #N B3LYP/6-31g(d) scf(xqc, novaracc) opt(MaxCycles=100)
4
5 b opt
6
7 +1 1
8 >>>>
9
10 >>>>

```

Note that you should modify `nproc` and `mem` for your machine.

Step 3: Run the global optimization:

```
nohup ../../isomer mol.inp > mol.out &
```

Note that this optimization is very expensive. During the optimization, there will be a directory named `mol-LM`, in which one can check the found local minima so far. Also, one can check the output file `mol.out`, where one can see the current energies. An example output is:

```

1 Will perform at most 30 calculations.
2 =====
3 #           Energy           Time     State
4 =====
5 0  -1028.04693646           397    Succeed
6 1   -899.91003266            51    Succeed
7 2  -1028.05070398           380    Succeed
8 3  -1027.95122573           173    Succeed
9 4  -1027.98390199           377    Succeed
10 5  -1028.08693656           219    Succeed
11 6  -1028.08350594           414    Succeed
12 7  -1027.94655101           357    Succeed
13 8  -1027.84124312           260    Succeed
14 9

```

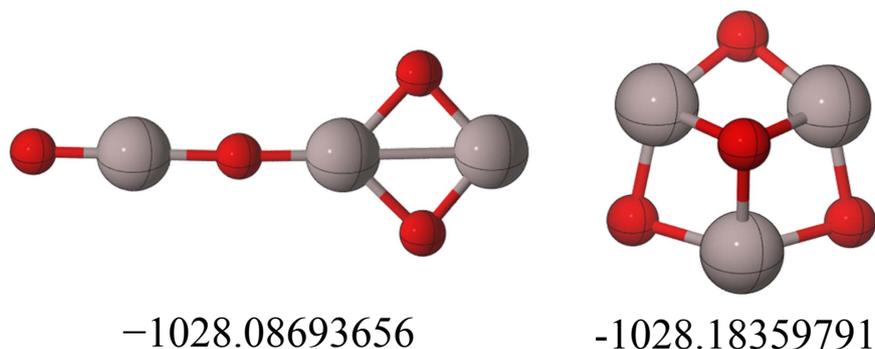
This means, the program is performing the 10th calculations. You can check the structure with low energy  $-1028.08693656$  by the file `mol-LM/5.xyz`. See Figure 5.2.1.

Step 4: After the optimization, you can check all the structures. There 27th structure has the lowest energy  $-1028.18359791$  and is the global minimum. You can check it from `27.xyz`. The structures are show in Figure 5.2.1.

### 5.2.3 More About optfile

Now we describe what `optfile` is. It is used by `xyz2gaussian` to convert a XYZ molecule into a Gaussian input file. Here is an example `optfile`. `xyz2gaussian` will put all the lines before the first >>>> in front of the coordinates, and all the lines between the two >>>> at the end of the coordinates, to generate a Gaussian input file.

In practise, you have to modify the charge, spin multiplicity, method, basis set, and other options to satisfy your requirement. Here `scf(xqc, novaracc)` is recommended

Figure 5.2.1: One local and global minimum of  $\text{Al}_3\text{O}_4^+$ .

since the initial guess can be very distorted, and this option can guarantee the convergence of the SCF calculations. For their meanings, please refer to the Gaussian manual.

#### 5.2.4 Example: $\text{Au}_6$

Now we want to know the global minimum of  $\text{Au}_6$ . Maybe you are thinking about the Gupta or Sutton–Chen potential. Unfortunately, for **small** metallic clusters, both potentials are very inaccurate[22]. Thus quantum chemistry must be used. Also, gold “enjoys” very strong relativistic effects. Thus one should use a suitable pseudopotential to describe gold. A good choice is the ECP60MDF. This pseudopotential can be obtained from <http://www.tc.uni-koeln.de/PP/clickpse.en.html>.

Step 1: In the ABCcluster distribution, go to the directory `testfiles/qc`. Create a file called `mol.inp`. For Windows users, the content should be:

```

1 mol          # Result file name
2 Au 6        # Symbols
3 plane 4 3   # Structure types
4 30         # Maximal number of calculations
5 >>>>
6 ../../xyz2gaussian optfile $inp$ > $xxx$.gjf
7 "D:\G09W\g09.exe" $xxx$.gjf
8 ../../gaussian2xyz $xxx$.out > $out$
9 >>>>

```

For Linux and Mac OS X users,

```

1 mol          # Result file name
2 Au 6        # Symbols
3 plane 4 3   # Structure types
4 30         # Maximal number of calculations
5 >>>>
6 ../../xyz2gaussian optfile $inp$ > $xxx$.gjf
7 g09 < $xxx$.gjf > $xxx$.log 2>/dev/null
8 ../../gaussian2xyz $xxx$.log > $out$
9 >>>>

```

Since I know that the global minimum of small gold clusters should be plane, I use `plane 4 3` for you to save time. In practise, however, when you do not know what the global minimum **should** be, you’d better use `cube` to search more kinds of structures.

Step 2: Create a file named `optfile` with the following content:

```
1 %nproc=20
2 %mem=400GB
3 #N TPSSTPSS/GENECP scf(xqc,novaracc) opt(Cartesian,
   MaxCycles=100)
4
5 b opt
6
7 0 1
8 >>>>
9 Au 0
10 S 8 1.00
11 0.38000800E+02 0.20009000E-01
12 0.23972500E+02 -0.15167900E+00
13 0.15218200E+02 0.36396000E+00
14 0.55399900E+01 -0.82132600E+00
15 0.13855100E+01 0.93664100E+00
16 0.64246100E+00 0.42352700E+00
17 0.15649600E+00 0.16250000E-01
18 0.54910000E-01 -0.97800000E-03
19 S 8 1.00
20 0.38000800E+02 -0.53040000E-02
21 0.23972500E+02 0.46318000E-01
22 0.15218200E+02 -0.11994000E+00
23 0.55399900E+01 0.30406200E+00
24 0.13855100E+01 -0.49450100E+00
25 0.64246100E+00 -0.25551600E+00
26 0.15649600E+00 0.60916300E+00
27 0.54910000E-01 0.59776700E+00
28 S 8 1.00
29 0.38000800E+02 0.32340000E-01
30 0.23972500E+02 -0.17176200E+00
31 0.15218200E+02 0.33950300E+00
32 0.55399900E+01 -0.74617900E+00
33 0.13855100E+01 0.19174980E+01
34 0.64246100E+00 -0.11299310E+01
35 0.15649600E+00 -0.13662840E+01
36 0.54910000E-01 0.14423910E+01
37 S 1 1.00
38 0.54910000E-01 0.10000000E+01
39 P 7 1.00
40 0.10309200E+02 0.12821700E+00
41 0.66276500E+01 -0.35379000E+00
42 0.16744700E+01 0.56621100E+00
43 0.80111600E+00 0.49317100E+00
44 0.34687900E+00 0.11377500E+00
45 0.12270100E+00 0.25340000E-02
46 0.42428000E-01 0.67900000E-03
47 P 7 1.00
48 0.10309200E+02 -0.35885000E-01
49 0.66276500E+01 0.10289000E+00
```

```

50 0.16744700E+01 -0.20098800E+00
51 0.80111600E+00 -0.20104500E+00
52 0.34687900E+00 0.11654900E+00
53 0.12270100E+00 0.59496900E+00
54 0.42428000E-01 0.45552000E+00
55 P 7 1.00
56 0.10309200E+02 -0.77242000E-01
57 0.66276500E+01 0.22261100E+00
58 0.16744700E+01 -0.49535300E+00
59 0.80111600E+00 -0.36074700E+00
60 0.34687900E+00 0.71000000E+00
61 0.12270100E+00 0.56883900E+00
62 0.42428000E-01 0.11930000E-02
63 P 1 1.00
64 0.42428000E-01 0.10000000E+01
65 D 6 1.00
66 0.11002700E+02 0.16467000E-01
67 0.68916600E+01 -0.68013000E-01
68 0.18080800E+01 0.29949200E+00
69 0.82105100E+00 0.45430300E+00
70 0.34416100E+00 0.34422400E+00
71 0.12974300E+00 0.12125600E+00
72 D 6 1.00
73 0.11002700E+02 -0.23628000E-01
74 0.68916600E+01 0.95672000E-01
75 0.18080800E+01 -0.54129400E+00
76 0.82105100E+00 -0.39553300E+00
77 0.34416100E+00 0.61916500E+00
78 0.12974300E+00 0.46827600E+00
79 D 1 1.00
80 0.12974300E+00 0.10000000E+01
81 F 1 1.00
82 0.89190000E+00 0.10000000E+01
83 ****
84
85 Au 0
86 ECP60MDF 5 60
87 H-Komponente
88 1
89 2 1.000000 0.000000
90 S-H
91 2
92 2 13.523218 426.641867
93 2 6.264384 36.800668
94 P-H
95 4
96 2 11.413867 87.002091
97 2 10.329215 174.004370
98 2 5.707424 8.870610
99 2 4.828165 17.902438
100 D-H

```

```

101 4
102 2 7.430963 49.883655
103 2 8.321990 74.684549
104 2 4.609642 6.486227
105 2 3.511507 9.546821
106 F-H
107 2
108 2 3.084639 8.791640
109 2 3.024743 11.658456
110 G-H
111 2
112 2 3.978442 -5.234337
113 2 4.011491 -6.738142
114
115 >>>>

```

Note that here we use TPSS/ECP60MDF method.

Step 3: Run the global optimization:

```
nohup ../../isomer mol.inp > mol.out &
```

Step 4: After the optimization, you can check the structures. For my run, the first structure (mol-LM/0.xyz) happens to be global minimum, which is shown in Figure 5.2.2.

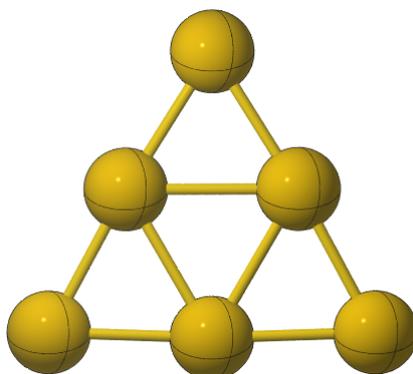


Figure 5.2.2: The global minimum of  $\text{Au}_6$ .

## 5.3 ABCluster with Other Programs

ABCluster can in principle work with any programs. Now we will see how to do this.

### 5.3.1 How does isomer work?

When `isomer` is running, it will generate a geometry with a long name, like `x-34`. You do not need to know its exact name, in ABCluster it can be represented by `$xxx$`. This geometry will be saved in standard XYZ format too a file named `x-34.xxxxxyz`, represented by `$inp$`. Then, commands between the two `>>>>` will be run one by one. Finally, the optimized geometry and energy should be written in XYZ format to a file named `x-34.ooooout` (The title line is the energy!), represented by `$out$`. Then `isomer`

will read optimized geometry and energy from this file and store it. then `isomer` will start next search. This mechanism can be show in Figure 5.3.1.

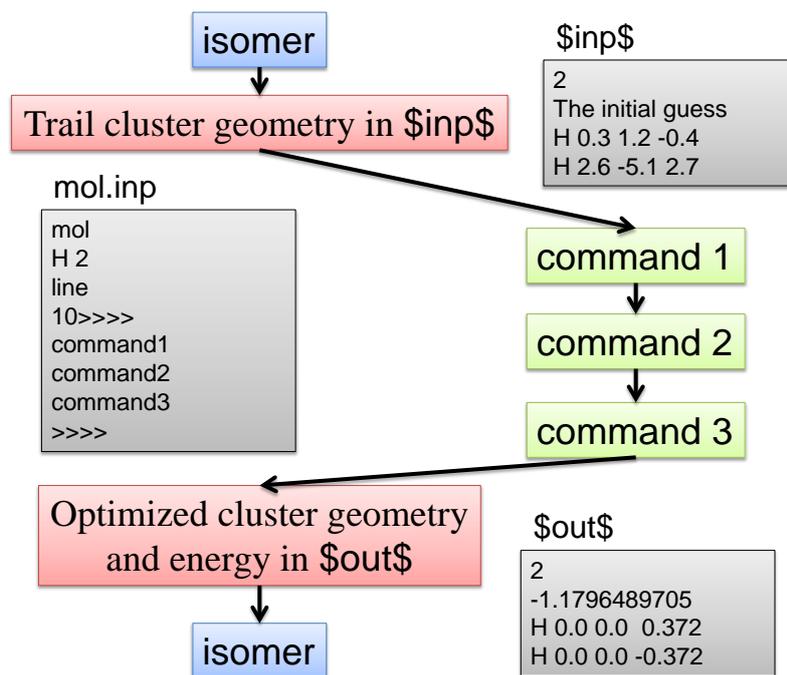


Figure 5.3.1: How `isomer` work with third-party programs.

Now let's see how we let `ABCluster` work with `Gaussian`. For the following commands:

```

>>>>
../../xyz2gaussian optfile $inp$ > $xxx$.gjf
g09 < $xxx$.gjf > $xxx$.log 2>/dev/null
../../gaussian2xyz $xxx$.log > $out$
>>>>
  
```

In the first line, `xyz2gaussian` use the structure (`$inp$`) generated by `isomer` and `optfile` to generate a `Gaussian` input file named `$xxx$.gjf`. The second line calls `Gaussian` to perform the local optimization, the output of which is in `$xxx$.log`. The third line extracts the final optimized structure and corresponding energy and saves it in `$out$`. This is exactly what Figure 5.3.1 instructs you to do.

In summary, your main task is to write a program or script to translate the XYZ format geometry into the format that the third-party program accepts, and perform the calculation, then extract energy and optimized geometry and save them in another XYZ file.

### 5.3.2 Example: `ABCluster` with `ORCA` on $\text{He}_2\text{Ne}_2$

Assuming you work in `Linux` and want to use `ORCA` to perform the quantum chemistry calculation. You want to know the global minimum of a very weakly bound cluster  $\text{He}_2\text{Ne}_2$ .

Step 1: In the `ABCluster` distribution, go to the directory `testfiles/qc`.

Step 2: In `Linux`, one can write a shell script to generate the input file, do the calculation, and extract the energy and geometry information. One possible script is:

```

1 #!/bin/bash
2
3 # Create input file
4 fn=$1-orca
5 xyzfn=$2
6 outfn=$3
7 echo "" ! B3LYP D3BJ TZVPP TZVPP/JK RIJCOSX TightSCF OPT
8 * xyz 0 1"" > ${fn}.inp
9 awk 'NR>2{print}' ${xyzfn} >> ${fn}.inp
10 echo "*" >> ${fn}.inp
11
12 # Run the calculation
13 /nfs/software/chemie/orca/3.0.3/linux_x86-64/orca ${fn}.inp
14 > ${fn}.out
15
16 # Transform the output file
17 energy='grep "Total Energy" ${fn}.out | tail -n 1 | awk '{
18 print $4}''
19 sed "2s/^\.*$/${energy}/" ${fn}.xyz > ${outfn}
20 rm -rf ${fn}.engrad ${fn}.gbw ${fn}.opt ${fn}.prop ${fn}.trj
21 ${fn}.xyz

```

If you are familiar with shell programming and ORCA input/output file format, this file is self-explaining. We call it as `oa`. Once create it, you must give an “executable” permission.

```
chmod +x oa
```

Step 2: Prepare a file called `mol.inp`:

```

1 mol          # Result file name
2 He 2 Ne 2    # Symbols
3 cube 2 2 2   # Structure types
4 10          # Maximal number of calculations
5 >>>>
6 ./oa $xxx$ $inp$ $out$
7 >>>>

```

Step 3: Run the optimization:

```
nohup ../../isomer mol.inp > mol.out &
```

Step 4: Check the output file `mol.out`, it seems that structure 3 is the most stable one, shown in Figure 5.3.2.

```

1 =====
2 #           Energy           Time    State
3 =====
4 0    -263.68047485           233    Succeed
5 1    -263.68100419           277    Succeed
6 2    -263.68070979           287    Succeed
7 3    -263.68123254           242    Succeed
8 4    -263.68029763           307    Succeed
9 5    -263.68116986           274    Succeed

```

10	6	-263.68101136	293	Succeed
11	7	-263.68053291	248	Succeed
12	8	-263.68026220	119	Succeed
13	9	-263.68019605	260	Succeed
14	=====			

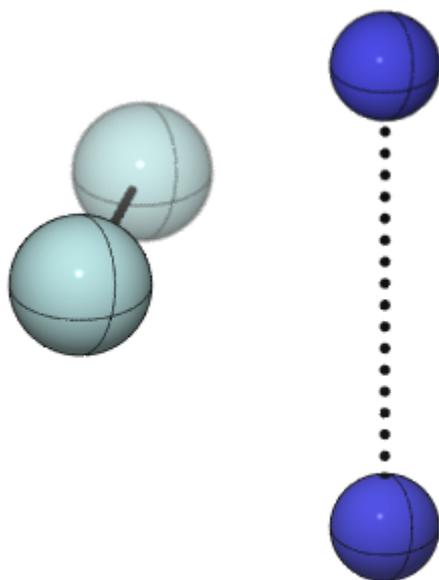


Figure 5.3.2: The global minimum of He<sub>2</sub>Ne<sub>2</sub>.

# Appendix A

## Version History

- Version 1.3 (Released on: Jan. 22, 2016): New algorithm has been introduced. Now the efficiency of multi-component atomic clusters (e.g.  $\text{Ag}_{14}\text{Cu}_{24}$ ) has been improved by 100 times!
- Version 1.2 (Released on: Nov. 6, 2015): The interfaces for third-party programs are available! Now ABCluster can do the global optimization with any quantum chemistry programs!
- Version 1.1 (Released on: Oct. 19, 2015): The optimization of Gupta and Sutton-Chen potential is significantly improved.
- Version 1.0 (Released on: Oct. 1, 2015): The first released version.



# Bibliography

- [1] J. Zhang, M. Dolg, ABCluster: The Artificial Bee Colony Algorithm for Cluster Global Optimization, *Phys. Chem. Chem. Phys.* **2015**, *17*:24173–24181.
- [2] J. Zhang, M. Dolg, Global Optimization of Clusters of Rigid Molecules Using the Artificial Bee Colony Algorithm, *Phys. Chem. Chem. Phys.* **2016**, *18*:3003–3010.
- [3] D. Liu, J. Nocedal, On the Limited Memory BFGS Method for Large Scale Optimization, *Math. Program.* **1989**, *45*(1-3):503–528.
- [4] M. J. Frisch, et al., *Gaussian*, Gaussian, Inc., Wallingford, CT.
- [5] F. Neese, The ORCA Program System, *Wiley Interdiscip. Rev.: Comput. Mol. Sci.* **2012**, *2*(1):73–78.
- [6] D. Karaboga, *An Idea Based on Honey Bee Swarm for Numerical Optimization*, Erciyes University: Technical Report TR06 **2005**.
- [7] M. Born, J. E. Mayer, Zur Gittertheorie der Ionenkristalle, *Z. Physik* **1932**, *75*(1-2):1–18.
- [8] J. Lennard-Jones, On the Determination of Molecular Fields, *Proc. R. Soc. Lond. A.* **1924**, *106*:463–477.
- [9] P. Morse, Diatomic Molecules According to the Wave Mechanics. II. Vibrational Levels, *Phys. Rev.* **1929**, *34*:57–64.
- [10] A. Pedone, G. Malavasi, M. C. Menziani, A. N. Cormack, U. Segre, A New Self-Consistent Empirical Interatomic Potential Model for Oxides, Silicates, and Silica-Based Glasses, *J. Phys. Chem. B* **2006**, *110*(24):11780–11795.
- [11] J. P. K. Doye, D. J. Wales, F. H. M. Zetterling, M. Dzugutov, The Favored Cluster Structures of Model Glass Formers, *J. Chem. Phys.* **2003**, *118*(6):2792–2799.
- [12] M. Dzugutov, Glass Formation in a Simple Monatomic Liquid with Icosahedral Inherent Local Order, *Phys. Rev. A* **1992**, *46*:R2984–R2987.
- [13] M. Dzugutov, Monatomic Model of Icosahedrally Ordered Metallic Glass Formers, *J. Non-Cryst. Solids* **1993**, *156-158*(0):173–176.
- [14] L. A. Girifalco, Molecular Properties of Fullerene in the Gas and Solid Phases, *The Journal of Physical Chemistry* **1992**, *96*(2):858–861.
- [15] R. P. Gupta, Lattice Relaxation at a Metal Surface, *Phys. Rev. B* **1981**, *23*:6265–6270.
- [16] A. P. Sutton, J. Chen, Long-range Finnis–Sinclair Potentials, *Phil. Mag. Lett.* **1990**, *61*(3):139–146.

- [17] G. V. Lewis, C. R. A. Catlow, Potential Models for Ionic Oxides, *J. Phys. C* **1985**, *18*(6):1149.
- [18] X. Lai, R. Xu, W. Huang, Geometry Optimization of Bimetallic Clusters Using an Efficient Heuristic Method, *J. Chem. Phys.* **2011**, *135*(16):164109.
- [19] J. A. D. MacKerell, D. Bashford, M. Bellott, J. R. L. Dunbrack, J. D. Evanseck, M. J. Field, S. Fischer, J. Gao, H. Guo, S. Ha, D. Joseph-McCarthy, L. Kuchnir, K. Kuczera, F. T. K. Lau, C. Mattos, S. Michnick, T. Ngo, D. T. Nguyen, B. Prodhom, W. E. Reiher, B. Roux, M. Schlenkrich, J. C. Smith, R. Stote, J. Straub, M. Watanabe, J. Wiórkiewicz-Kuczera, D. Yin, M. Karplus, All-atom Empirical Potential for Molecular Modeling and Dynamics Studies of Proteins, *J. Phys. Chem. B* **1998**, *102*(18):3586–3616.
- [20] W. L. Jorgensen, D. S. Maxwell, , J. Tirado-Rives, Development and Testing of the OPLS All-atom Force Field on Conformational Energetics and Properties of Organic Liquids, *J. Am. Chem. Soc.* **1996**, *118*(45):11225–11236.
- [21] W. D. Cornell, P. Cieplak, C. I. Bayly, I. R. Gould, K. M. Merz, D. M. Ferguson, D. C. Spellmeyer, T. Fox, J. W. Caldwell, P. A. Kollman, A Second Generation Force Field for the Simulation of Proteins, Nucleic Acids, and Organic Molecules, *J. Am. Chem. Soc.* **1995**, *117*(19):5179–5197.
- [22] A. Hermann, R. P. Krawczyk, M. Lein, P. Schwerdtfeger, I. P. Hamilton, J. J. P. Stewart, Convergence of the Many-body Expansion of Interaction Potentials: From van der Waals to Covalent and Metallic Systems, *Phys. Rev. A* **2007**, *76*:013202.